## LOK JAGRUTI UNIVERSITY (LJU)

## INSTITUTE OF ENGINEERING AND TECHNOLOGY

## **Department of Artificial Intelligence and Machine Learning (704)**

## **Bachelor of Engineering (B.E.) – Semester – II**

| Course Code:                | 017041291                   |  |  |
|-----------------------------|-----------------------------|--|--|
| Course Name:                | Mathematics - II            |  |  |
| Category of Course:         | Basic Science Course (BSC)  |  |  |
| <b>Prerequisite Course:</b> | Mathematics - I (017041191) |  |  |

| <b>Teaching Scheme</b> |              |               |        |                |
|------------------------|--------------|---------------|--------|----------------|
| Lecture<br>(L)         | Tutorial (T) | Practical (P) | Credit | Total<br>Hours |
| 3                      | 2            | 0             | 5      | 50             |

|             | S  | yllabus                       |                              |                   |  |  |  |
|-------------|--|-------------------------------|------------------------------|-------------------|--|--|--|
| Unit<br>No. | Topic  | Prerequisite Topic            | Successive Topic             | Teaching<br>Hours |  |  |  |
|             | Matrices   |                               |                              |                   |  |  |  |
|             | 1.1 Elementary row operations of matrices Divide & Conquer (017043591-   |                               |                              |                   |  |  |  |
|             | 1.2 Row and reduced row echelon form   |                               | Unit-3)                      |                   |  |  |  |
|             | 1.3 System of linear equations   |                               |                              | _                 |  |  |  |
| 01          | 1.4 Homogeneous system of linear equations   |                               | _                            | (14%)             |  |  |  |
| VI.         | 1.5 Non-homogeneous system of linear equations   |                               | Cryptography(017043791-Unit- | (14/0)            |  |  |  |
|             | 1.6 Inverse of Matrix (Using Gauss-Jordan Method)  |                               | 2)                           |                   |  |  |  |
|             | 1.7 Eigen values & vectors   | E                             |                              | -                 |  |  |  |
|             | 1.8 Diagonalization of matrix (Only for Non-symmetric Matrix)  | Factorization(017041191-Unit- |                              |                   |  |  |  |
|             | 1.9 Cayley-Hamilton theorem  | 1)                            |                              |                   |  |  |  |
|             | Fourier Series   |                               |                              |                   |  |  |  |
|             | 2.1 Periodic function  |                               |                              | 5                 |  |  |  |
|             | 2.2 Dirichlet's condition  |                               |                              | (10%)             |  |  |  |
| 02          | 2.3 Trigonometric series of sine and cosine function   | Basic integration (017041191- |                              | (1070)            |  |  |  |
|             | 2.4 Fourier series of a function of period 2L  | Unit-3)                       |                              |                   |  |  |  |
|             | 2.5 Fourier series of even and odd function  |                               |                              | -                 |  |  |  |
|             | 2.6 Half range expansions  |                               |                              |                   |  |  |  |
|             | Some Special Functions   | ,                             |                              |                   |  |  |  |
|             | 3.1Gamma function, Beta function. (And its Properties)   |                               |                              | <u> </u>          |  |  |  |
|             | 3.2 Bessel function, Dirac's Delta function (Definition only)  |                               |                              | -                 |  |  |  |
| 03          | 3.3 Error function and complementary Error function (Definition  |                               |                              | 4                 |  |  |  |
|             | only)  2.4 Hasviside's function, mules which height and dynation function.                                     |                               |                              |                   |  |  |  |
|             | 3.4 Heaviside's function, pulse unit height and duration function (Definition only)                            |                               |                              | (8%)              |  |  |  |
|             | 3.5 Rectangle function, Gate function (Definition only)  |                               |                              | (0,0)             |  |  |  |
|             | 3.6 Signum function, Saw tooth wave function (Definition only)   |                               |                              | _                 |  |  |  |
|             | 3.7 Triangular wave function, Halfwave rectified sinusoidal  |                               |                              | -                 |  |  |  |
|             | function, Full rectified sine wave, Square wavefunction.   |                               |                              |                   |  |  |  |
|             | (Definition only)  |                               |                              |                   |  |  |  |
|             | Fourier Integral and Fourier Transform   |                               |                              |                   |  |  |  |
|             | 4.1 Define Fourier integral  |                               |                              | 4                 |  |  |  |
| 04          | 4.2 Cosine and sine integral   | Basic integration (017041191- |                              | (8%)              |  |  |  |
|             | 4.3 Define Fourier transform   | Unit-3)                       |                              | -                 |  |  |  |
|             | 4.4 Cosine and sine transform  |                               |                              |                   |  |  |  |
|             | First Order Ordinary Differential Equations  |                               |                              |                   |  |  |  |
|             | 5.1 Geometric meaning of $y' = f(x, y)$ direction fields   |                               |                              | 5                 |  |  |  |
| 05          | 5.2 Exact differential equations and integrating factor  | <b>5</b>                      |                              | (10%)             |  |  |  |
|             | 5.3 Linear differential equations  | Basic differentiation &       |                              | -                 |  |  |  |
|             | 5.4 Bernoulli equations  | integration(017041191-Unit-3) |                              |                   |  |  |  |
|             | <b>Higher Order Ordinary Differential Equations</b>  |                               |                              | _                 |  |  |  |
|             | 6.1 Linear differential equations of second and higher order   |                               |                              | _                 |  |  |  |
|             | 6.2 Homogeneous linear differential equations of higher order  |                               |                              | -                 |  |  |  |
|             | <ul><li>6.3 Higher order non-homogeneous equations</li><li>6.4 Solution by undetermined coefficients</li></ul> | Factorization(017041191-Unit- |                              | _                 |  |  |  |
|             | 6.5 Solution by variation of parameters  | 1)                            |                              | _                 |  |  |  |
|             | 6.6 Solution by [1/f(D)] r(x) method for finding particular  | <u>'</u>                      |                              | -                 |  |  |  |
| 06          | integral.  |                               |                              | (14%)             |  |  |  |
| vv          | 6.7 Ordinary differential equations with variable coefficient  | Solution by undetermined      |                              | (17/0)            |  |  |  |
|             | (Reducible to constant coefficient) (Cauchy-Euler's &  | coefficients (017041291-Unit- |                              |                   |  |  |  |
|             | Legendre's Equation)   | 6), Solution by [1/f(D)] r(x) |                              |                   |  |  |  |
|             |  | method for finding particular |                              |                   |  |  |  |
|             |  | integral (017041291-Unit-6)   |                              |                   |  |  |  |
|             |  |                               |                              |                   |  |  |  |
|             |  |                               |                              |                   |  |  |  |

|    | Modeling of Ordinary Differential Equations                       |  |               |
|----|---|--|---------------|
| 07 | 7.1 Orthogonal trajectories of curves (Only Cartesian Curves)     | First order ordinary differential equations (017041291-Unit-5) | <br>3<br>(6%) |
| 07 | 7.2 Oscillations and resonance (For undamped Forced Oscillations) | Higher order ordinary differential equations                   | <br>(0%)      |
|    | 7.3 Modeling: Electric Circuits (Only RLC-Circuit)                | (017041291-Unit-6)   |               |
|    | Power Series  |  |               |
|    | 8.1 Classification of singularities                               |  | <br>5         |
| 08 | 8.2 Series solution near ordinary points                          |  | <br>(10%)     |
|    | 8.3 Series solution near regular singular points                  |  |               |
| 1  | (Frobenius Method)  |  |               |
|    | Laplace Transform   |  |               |
|    | 9.1 Laplace transform of elementary functions                     |  |               |
|    | 9.2 Differentiation of Laplace transform                          |  |               |
|    | 9.3 Integration of Laplace transform                              |  | <br>7         |
| 09 | 9.4 Laplace transform of derivatives                              | Basic differentiation &  | <br>(14%)     |
|    | 9.5 Laplace transform of integrals                                | integration(017041191-Unit-3)                                  |               |
|    | 9.6 Unit step function and Dirac's delta function                 |  |               |
|    | 9.7 Inverse Laplace transform                                     |  |               |
|    | 9.8 Convolution theorem   |  |               |
|    | Application of Laplace Transform                                  |  |               |
|    |   | Laplace transform of   |               |
| 10 | 10.1 Solution of linear ordinary differential equation            | elementary functions, Laplace                                  | 3             |
|    |   | transform of derivatives, Unit                                 | (6%)          |
|    |   | step function and Dirac's delta                                | <br>(5,5)     |
|    | 10.2 Solution of simultaneous equations                           | function, Inverse Laplace                                      |               |
|    |   | transform, Convolution   |               |
|    |   | theorem(017041291-Unit-9)                                      |               |

| Proposed Theory + Practical Evaluation Scheme by Academicians (% Weightage Category Wise and it's Marks Distribution) |                   |         |  |  |  |
|---|-------------------|---------|--|--|--|
| L: 2 P: 0   |                   |         |  |  |  |
| **  | 7D 4 1 4 7D 4 7D4 | me me m |  |  |  |

Note: In Theory Group, Total 4 Test (T1+T2+T3+T4) will be conducted for each subject. Each Test will be of 25 Marks. Each Test Syllabus Weightage: Range should be 20% - 30%

| Each Test Synabus Weightage. Range should be 2070 - 5070 |                                       |                            |                                     |             |                 |
|--|---------------------------------------|----------------------------|-------------------------------------|-------------|-----------------|
| Group (Theory or<br>Practical)                           | Group (Theory or<br>Practical) Credit | Total<br>Subject<br>Credit | Category                            | % Weightage | Marks Weightage |
| Theory   |                                       |                            | MCQ                                 | 15%         | 15              |
| Theory   | 5                                     |                            | Theory Descriptive                  | 0%          | 0               |
| Theory   | 5                                     |                            | Formulas and Derivation             | 10%         | 10              |
| Theory   |                                       |                            | Numerical                           | 75%         | 75              |
| Expected Theory %  | 100%                                  | 5                          | Calculated Theory %                 | 100%        | 100             |
| Practical  |                                       | J                          | Individual Project                  | 0%          | 0               |
| Practical  |                                       |                            | Group Project                       | 0%          | 0               |
| Practical  | 0                                     |                            | Internal Practical Evaluation (IPE) | 0%          | 0               |
| Practical  |                                       |                            | Viva                                | 0%          | 0               |
| Practical  |                                       |                            | Seminar                             | 0%          | 0               |
| Expected Practical %                                     | 0%                                    |                            | Calculated Practical %              | 0%          | 0               |
| Overall %  | 100%                                  |                            |                                     | 100%        | 100             |

| Cours | se Outcome   |
|-------|--|
|       | Upon completion of the course students will be able to   |
| CO1   | Understand and apply matrix operation and properties, solve systems of linear equations using matrices, analyze systems using eigen values and eigne   |
|       | vectors, apply matrices in signal processing tasks, Explain the concept of Fourier series and its properties, Apply Fourier series in digital          |
|       | communications and image processing also in control system analysis.   |
| CO2   | Design filter and modulation schemes and Implement algorithms like FFT for efficient computation of Fourier transforms, Apply Bessel functions and     |
|       | other special function to solve engineering problems. Solve first order & first degree ODEs using various methods.                                     |
| CO3   | Solve higher order linear ODEs using various methods such as undetermined coefficients, variation of parameters. Formulate ODEs from real-world        |
|       | engineering problems. Apply knowledge of ODEs to design and analyze systems in computer engineering domains. Apply orthogonal trajectories in          |
|       | edge detection algorithms for image processing and utilize for curve fitting and surface modeling in computer graphics. Understand the significance of |
|       | ordinary and singular points in ODEs.  |
| CO4   | Understand and apply Laplace transforms to solve linear ODEs with constant coefficients. Apply knowledge to real-world engineering problems,           |
|       | especially in signal processing, circuit analysis, control system and system modeling.   |
| Sugge | ested Reference Books  |
| 1     | Elementary Linear Algebra, Applications version, Anton and Rorres, Wiley India Edition.  |
| 2     | Advanced Engineering Mathematics, Erwin Kreysig, Wiley Publication.  |
| 3     | Advanced Engineering Mathematics, Dennis G. Zill, 4 <sup>th</sup> edition, Jones and Bartlett Publishers.  |
| 4     | Higher Engineering Mathematics, B.S.Grewal, Khanna Publishers.   |

| List o | List of Open Source Software/Learning website |  |  |
|--------|---|--|--|
| 1      | https://nptel.ac.in                           |  |  |